

- Design provision for Rebar End Anchorage Theory in EN 1992-1-1 (2004)
- Introduction to design provision for Bonded Anchor Theory in EN 1992-4 (2018)
- 4. Introduction to strut-and-tie model
- 5. Notes on seismic actions
- 6. Conclusion

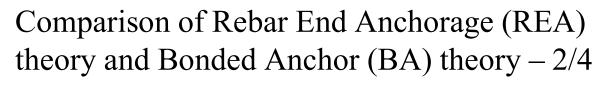
1. Design	philosophy of post-in	nstalled rebar (PIR)
Prequalification:	EOTA EAD 330087 (2018)	EOTA EAD 330499 (2017) (formerly ETAG 001, part 5, 2006)
Design:	Design as cast-in rebar end anchorage	Design as bonded anchors
Standards:	EN 1992-1-1 (2004) or locally MS EN 1992-1-1 (2010)	EN 1992-4 (2018) (formerly EOTA TR 045, 2013)
	(commonly known as EC2)	3

## International design standards

Document	Organisation	<b>Roles and functions</b>	Remarks
EN 1992-1-1 (2004) or MS EN 1992-1-1 (2010)	European Committee for Standardization (CEN) or Standards Malaysia	General reinforced concrete design in Europe.	Design provisions for anchorage and splice length in Chapter 8.
ACI 318 (2014)	ACI	General reinforced concrete design in US.	Design provisions for development length (rebar theory) in Chapter 25, and anchor theory in Chapter 17.
EOTA TR 045 (2013)	ΕΟΤΑ	Guideline for design of post-installed anchor theory design in Europe.	Superseded by EN 1992-4 (2018)
EN 1992-4 (2018)	CEN	Standard for design of post-installed anchor theory design in Europe.	
BS 8539 (2012) The British Standards Institution (BSI)		Selection and installation of post- installed anchors in UK.	Recommendations for anchors without European Technical Approvals (ETAs) qualification

# Comparison of Rebar End Anchorage (REA) theory and Bonded Anchor (BA) theory – 1/4

Main difference	<b>REA theory</b>	<b>BA theory</b>
	Static action and fire	
	exposure:	Static action:
	EOTA EAD 330087 (2018)	EAD 330499 (2017)
Prequalification		
documents	Seismic action:	Seismic action:
	EAD 331522 (endorsed draft	EOTA
	2018)	TR 045 (2013)
		× ,
	Static action: Chapter 8 in EN	
	1992-1-1 (2004) or MS EN	
	1992-1-1 (2010)	
Desien stendend		EN 1002 4 (2019)
Design standard	Seismic action: Chapter 5.6 in	EN 1992-4 (2018)
	EN 1998-1 (2004) or MS	
	EN1998-1 (2015)	



Main difference	<b>REA theory</b>	BA theory
	Equilibrium with local or global concrete struts, may	
Load transfer mechanism	require the supplement of transverse reinforcement in lapping splices.	Utilisation of tensile concrete strength

Cast-in rebar with lap splice	Table 3.	1 Str	rength	and	deforn	natior	n chara	acteris	stics fe	or con	crete						
Star and Start						Streng	gth cla	isses	for co	ncrete						Analytical relation / Explanation	BS E EN 1
	f <sub>ck</sub> (MPa)	12	16	20	25	30	35	40	45	50	55	60	70	80	90		EN 1992 1992-1-1
show	f <sub>ck,cube</sub> (MPa)	15	20	25	30	37	45	50	55	60	67	75	85	95	105	2.8	)2-1-1: -1:200
	/ <sub>cm</sub> (MPa)	20	24	28	33	38	43	48	53	58	63	68	78	88	98	$f_{cm} = f_{ck} + 8(MPa)$	2-1-1:2004 1:2004 (E)
	f <sub>ctm</sub> (MPa)	1,6	1,9	2,2	2,6	2,9	3,2	3,5	3,8	4,1	4,2	4,4	4,6	4,8	5,0	$f_{ctm}$ =0,30× $f_{ct}$ <sup>(20)</sup> ≤C50/60 $f_{ctm}$ =2,12·In(1+( $f_{cm}$ /10)) > C50/60	
	f <sub>ctk, 0,05</sub> (MPa)	1,1	1,3	1,5	1,8	2,0	2,2	2,5	2,7	2,9	3,0	3,1	3,2	3,4	3,5	$f_{cb:0,05} = 0.7 \times f_{cbm}$ 5% fractile	

Adhesive

Tension

Concrete

# Comparison of Rebar End Anchorage (REA) theory and Bonded Anchor (BA) theory -3/4

Main difference	<b>REA theory</b>	BA theory
Failure modes	<u>Tension</u> : steel failure, pull out, splitting (near to the	<u>Tension</u> : steel failure, concrete breakout (cone failure), bond failure (pull-out failure), splitting (near to the edge);
	edge)	Shear: steel failure, concrete breakout and concrete pryout
Tension	Tension Tension	Tension Tension
	Ne	
Steel failure	Pull-out Splitting	Bond failure Breakout failure <b>7</b>

# Comparison of Rebar End Anchorage (REA) theory and Bonded Anchor (BA) theory – 4/4

Main difference	<b>REA theory</b>	BA theory
Provision to base material	Uncracked concrete	Cracked and uncracked concrete
Design results	Reinforcement length	Strength capacity
Allowable embedment length $(l_b)$	$\max \{0.3 \ l_{b,rqd}; 10\phi; 100 \text{ mm} \}$ $\leq l_b \leq 60\phi$ $(\phi \text{ is the rebar diameter})$	$6\phi \le l_{\rm b} \le 20\phi$ ( $\phi$ is the rebar diameter)

## Some latest development for Europe

Engineering Structures 100 (2015) 645-655



Contents lists available at ScienceDirect

#### **Engineering Structures**

journal homepage: www.elsevier.com/locate/engstruct

Design of post-installed reinforcing bars as end anchorage or as bonded anchor

Christoph Mahrenholtz\*, Rolf Eligehausen, Hans-Wolf Reinhardt

University of Stuttgart, Pfafferwaldring 4, 70569 Stuttgart, Germany

## Some latest development for US

ACI STRUCTURAL JOURNAL

#### **TECHNICAL PAPER**

Title no. 110-S34

#### Recommended Procedures for Development and Splicing of Post-Installed Bonded Reinforcing Bars in Concrete Structures

by Finley A. Charney, Kamalika Pal, and John Silva

ACI Structural Journal, V. 110, No. 3, May-June 2013. MS No. S-2011-182.R2 received September 29, 2011, and reviewed under Institute publication policies. Copyright © 2013, American Concrete Institute. All rights reserved, including the making of copies unless permission is obtained from the copyright proprietors. Pertinent discussion including author's closure, if any, will be published in the March-April 2014 ACI Structural Journal if the discussion is received by November 1, 2013.

CrossMark

## Content

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11

2. Design provision for Rebar End Anchorage Theory in EN 1992-1-1 (2004)

## Longitudinal bar anchorage (Cl. 8.4)

Cl. 8.4.2 (2): Design value of ultimate bond stress,  $f_{bd} = 2.25 \eta_1 \eta_2 f_{ctd}$ Where,

Concrete design tensile strength ( $f_{ctd}$ ) = 5% fractile with consideration of partial safety factor ( $f_{ctd} = f_{ctk,0.05}/\gamma_m$ );

 $\eta_1$  and  $\eta_2$  are to implicitly account for bond condition, position of rebar and rebar diameter.

BS 8110,  $f_{bu} = \beta \sqrt{f_{cu}}$  $\beta = 0.5$  tens; 0.63 comp for Type 2 deformed bar Note that  $\beta$  includes  $\gamma_m = 1.4$ 

Basic derivation of anchorage length  $(l_b)$   $F_{bond} \ge F_{rebar}$   $f_{bd} A_{s,surface} \ge f_{rebar} A_s$   $f_{bd}(\pi\phi)l_b \ge f_{rebar}\left(\frac{\pi\phi^2}{4}\right)$   $l_b \ge \frac{f_{rebar}\phi}{f_{bd}4}$  Design yield strength of rebar  $l_{bd} \ge \frac{0.87f_{yk}\phi}{f_{bd}4}$  (BS 8110)  $l_{b,rqd} \ge \frac{\sigma_{sd}\phi}{f_{bd}4}$  (EN 1992-1-1)

# Further checking procedure on the design anchorage length $(l_{bd})$

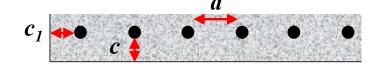
Bars form (for straight bars,  $\alpha_1$  is 1.0)  $l_{bd} = \alpha_1 \alpha_2 \alpha_3 \alpha_5 l_{b,rqd} \ge l_{min}$ Confinement effect

•  $\alpha_2$  is a coefficient for the effect of concrete minimum cover to consider splitting failure for straight bars.

$$0.7 \le \alpha_2 = 1 - \frac{0.15(c_d - \phi)}{\phi} \le 1.0$$
 (Tension)

 $\alpha_2 = 1.0$  (Compression)

where  $c_d = \min \{a/2, c_1, c\}$  for straight bars, *s* is the clear spacing of bars,  $c_1$  is the side cover and *c* is the top or bottom cover.



## Splitting failure and $\alpha_2$

 Splitting is the failure of the concrete surrounding the anchorage because of excessive radial stresses.

Figure taken from:

Randl, N. and Kunz, J (2014), Post-installed reinforcement connections at ultimate and serviceability limit states, Structural

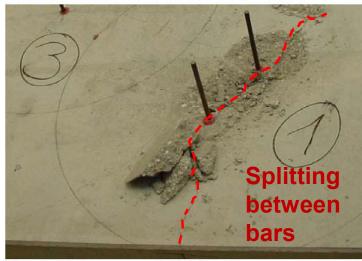
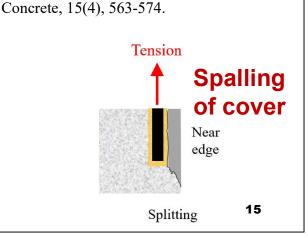
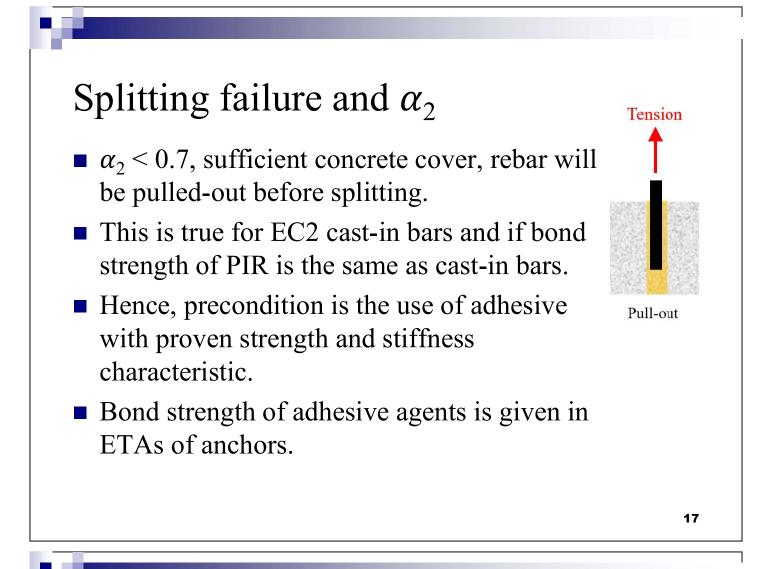


Figure 5: Splitting tests with double bars



## Splitting failure and $\alpha_2$

- Since splitting is a pure concrete failure, the design of post-installed bars should respect the same splitting criteria as cast-in bars.
- As long as  $\alpha_2 \ge 0.7$  (correspond to cover  $c_d \le 3\phi$ ), splitting of concrete cover occurs.
- It should be noted that the case of  $\alpha_2 = 1.0$ corresponds to a concrete cover  $c_d$  of  $1\phi$ , which present challenges in hole drilling – need to account for possible deviation in drilling, hence a minimum concrete cover  $c_d$  of  $2\phi$ , corresponds to  $\alpha_2 = 0.85$ should be taken.



What if the bond strength of PIR is proven stronger than cast-in rebar? – an extension of EC2

• Extrapolate  $\alpha_2$  linearly for  $c_d \ge 3$ , following the approach of Tepfers (1973), hence:

• 
$$\alpha_2 = 1 - \frac{0.15(c_d - \phi)}{\phi}$$
 in EC2 becomes

• 
$$\alpha'_2 = \frac{1}{\frac{1}{0.7} + \delta \frac{c_d - 3\phi}{\phi}} \ge 0.25$$

•  $\delta$  is a factor calibrated by test, if linearly continues with the same slope,  $\delta = 0.15$ .

Tepfers, R. 1973. A Theory of Bond Applied to Overlapped Tensile Reinforcement for Deformed Bars. Chalmers University, Göteborg. No 73/2.

## Summary of bond strength in accordance to REA theory in EN 1992-1-1 (2004)

Concrete characterist	Concrete characterist			trength in MPa)		Bond strength (Compression in MPa)				
ic cube strength, $f_{cu,k}$ (MPa)	ic tensile strength at 5% fractile, $f_{ctk,0.05}$ (MPa)	BS 8110 ( $\beta = 0.5$ )	EC2 (norma lised by $\alpha_2$ = 0.7)	EC2 (norma lised by $\alpha_2$ = 0.85)	EC2 (normali sed by $\alpha_2 =$ 1.0)	BS 8110 ( $\beta = 0.63$ )	EC2 (normalise d by $\alpha_2 =$ 1.0)			
25	1.5	3.5	4.8	4.0	3.4	4.4	3.4			
30	1.8	3.8	5.8	4.8	4.1	4.8	4.1			
40	2.1	4.4	6.7	5.5	4.7	5.6	4.7			
50	2.5	4.9	8.0	6.6	5.6	6.2	5.6			
60	2.9	5.4	9.3	7.7	6.5	6.8	6.5			

Note: Material safety factor was excluded

19

## Minimum anchorage length $(l_{b,min})$

 $l_{b,min} \ge \max\{0.3l_{b,rqd}, 10\phi, 100 \text{ mm}\}$  (Tension)

 $l_{b,min} \ge \max\{0.6l_{b,rqd}, 10\phi, 100 \text{ }mm\}$  (Compression)

It should be noted that the minimum anchorage length ( $I_{min}$ ) shall be multiplied by an amplification factor ( $\alpha_{lb}$ ) to account for the difference of cast-in place and post-installed rebar in cracked concrete. In general, if there is no test carried out to post-installed rebars in cracked concrete in accordance to qualification document EOTA EAD 330087 (2018),  $\alpha_{lb}$ 

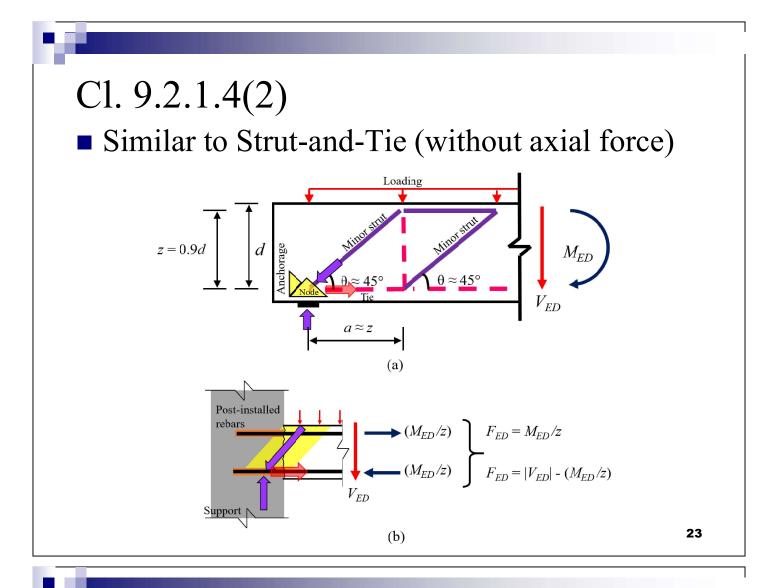
is taken as 1.5.

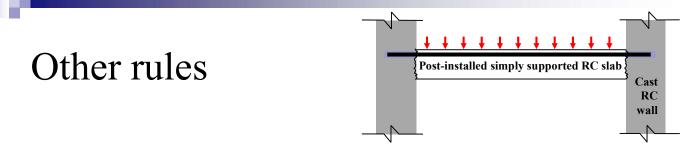
Lapped splice 
$$(l_o)$$
  
 $l_o = \alpha_1 \alpha_2 \alpha_3 \alpha_5 \alpha_6 l_{b,rqd} \ge l_{o,min}$   
Where,  $\alpha_6$  is a coefficient of percentage of lapped  
bar  $(p_1)$  relative to total cross-section area within  
 $0.65l_o$  from the centre of the lap length  
 $1.0 \le \alpha_6 = (\rho_1/25)^{0.5} \le 1.5$   
 $l_{o,min} \ge \max\{0.3\alpha_6 l_{b,rqd}, 15\phi, 200 \text{ mm}\}$   
21  
Cher rules  
C1. 9.2.1.2(1) and C1. 9.2.1.4(1):

 Values of 15% of maximum bending moment in the span and 25% (National Annex dependent, in contrast, it is 50% in BS 8110) of the steel area provided in the span is recommended for top and bottom reinforcement, respectively, at the support of simply supported beam.

Simply supported beam

Both top and bottom steel are to be anchored with  $l_{bd}$ , measured from the face of support. It is interesting to note that Cl. 9.2.1.4(2) allows a strut-and-tie equivalent model to calculate the axial forces in the rebar, which appears to be more suitable for the design stress  $(\sigma_{sd})$  estimation in  $l_{b,rqd} \ge \frac{\sigma_{sd}}{f_{bd}}\frac{\phi}{4}$ 



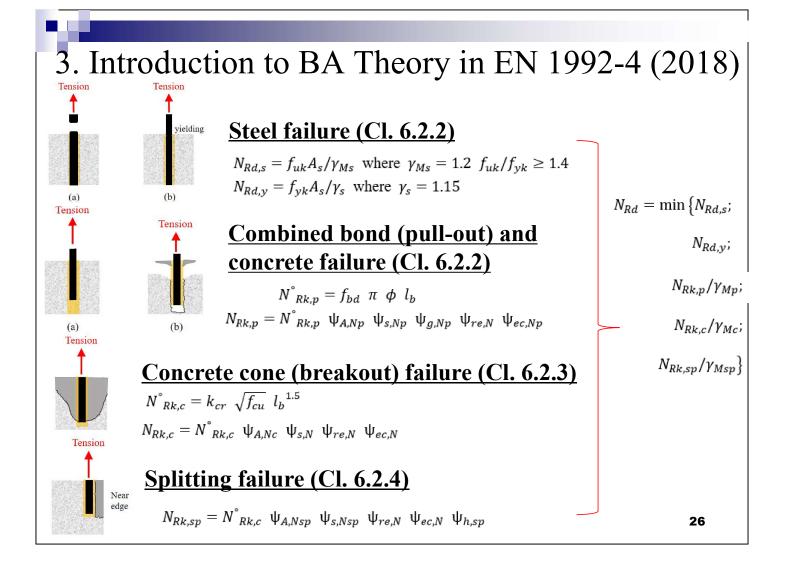


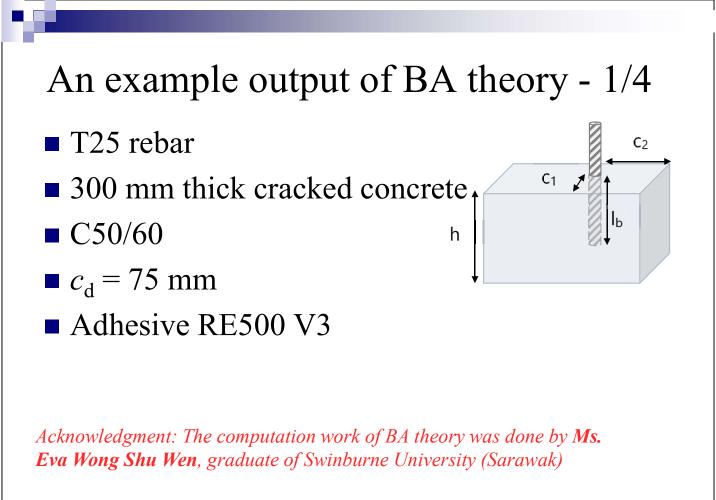
### Cl. 9.3.1.2: Simply supported solid slab

- In simply supported slab, 15% (for end support) to 25% (intermediate support) of maximum bending moment in the span and 50% of the calculated span reinforcement should be provided for the top and bottom bar at the support of solid slab, respectively (as opposed to the 50% provision in BS 8110).
- Both top and bottom steel are anchored with *l<sub>bd</sub>*, measured from the face of support. Similar for simply supported beam, Cl. 9.2.1.4(2) of the strut-and-tie model is allowed.

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- 4. Introduction to strut-and-tie model
- 5. Notes on seismic actions
- 6. Conclusion

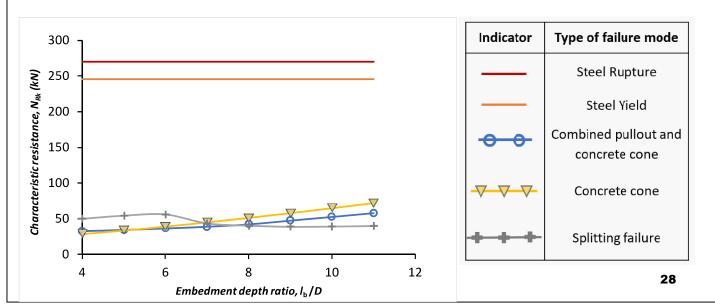


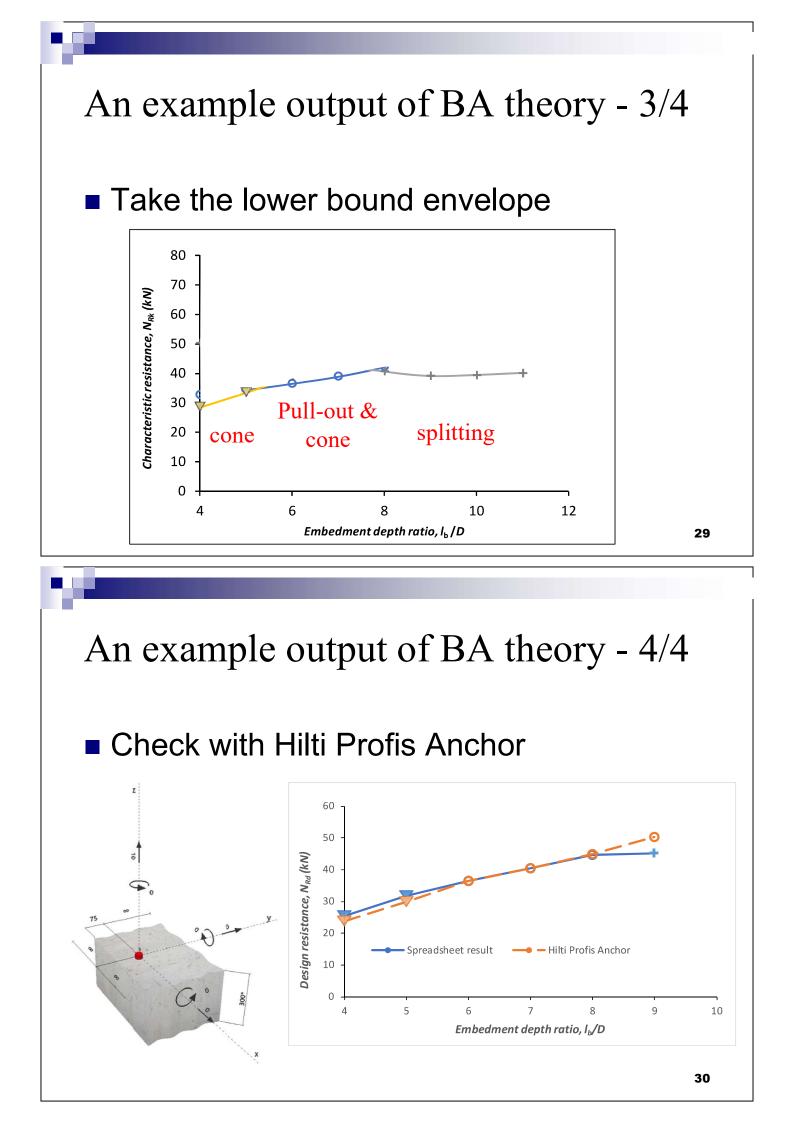


27

## An example output of BA theory - 2/4

l <sub>b</sub> /D	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
N <sub>Rd,s</sub> (kN)	269.98	269.98	269.98	269.98	269.98	269.98	269.98	269.98	269.98	269.98	269.98	269.98	269.98	269.98	269.98	269.98	269.98
N <sub>Rd,y</sub> (kN)	245.44	245.44	245.44	245.44	245.44	245.44	245.44	245.44	245.44	245.44	245.44	245.44	245.44	245.44	245.44	245.44	245.44
N <sub>Rk,p</sub> (kN)	32.75	34.40	36.53	38.92	42.29	47.57	52.86	58.15	63.43	68.72	74.00	79.29	84.58	89.86	95.15	100.44	105.72
N <sub>Rk,c</sub> (kN)	28.52	33.49	38.96	44.83	51.07	57.64	64.50	71.66	79.09	86.79	94.73	102.92	111.34	119.99	128.87	137.96	147.25
N <sub>Rk,sp</sub> (kN)	50.20	54.67	56.28	43.79	40.59	39.04	39.42	40.13	40.83	41.53	42.21	42.88	43.54	44.17	44.80	45.41	46.01



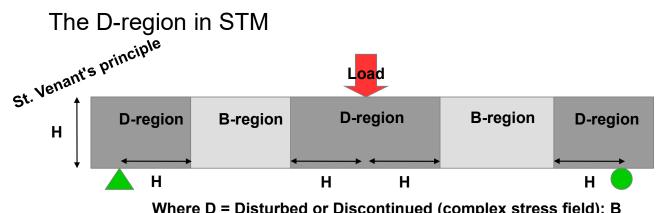


## Content

- Design philosophy of PIR 1.
- Design provision for Rebar End Anchorage Theory in EN 2. 1992-1-1 (2004)
- 3. Introduction to design provision for Bonded Anchor Theory in EN 1992-4 (2018)
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- Notes on seismic actions 5.
- Conclusion 6.

31

## 4. Introduction to Strut-and-Tie Method (STM)



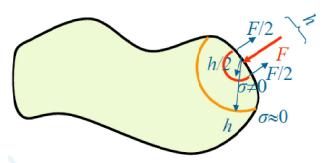
Where D = Disturbed or Discontinued (complex stress field); B = Bernoulli (linear strain, plane section remains plane)

Brief history and background:

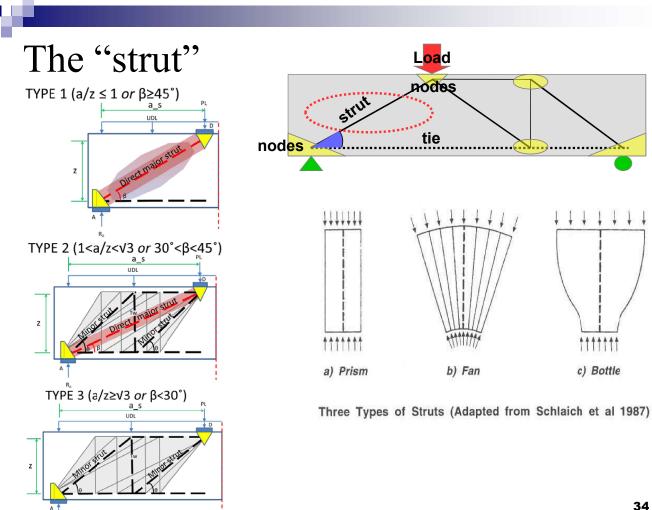
- Schlaich et al. (1987), Collins and Mitchell (1991), MacGregor (1992), Foster and Gilbert (1996), Tjhin and Kuchma (2002)
- Lower bound plastic theory (equilibrium and yield criteria for rigid perfectly plastic) – modified with efficiency factor v, and crushing of concrete does not happen prior to yield of rebars 32

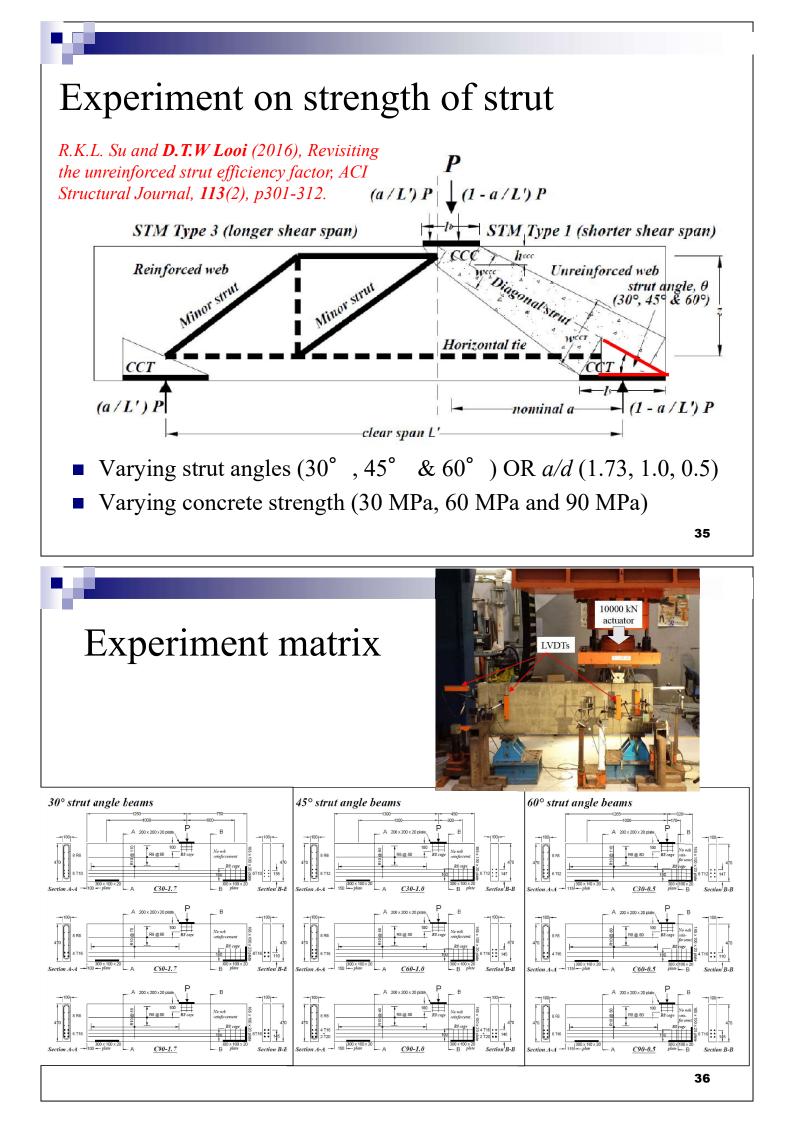
## St. Venant principle

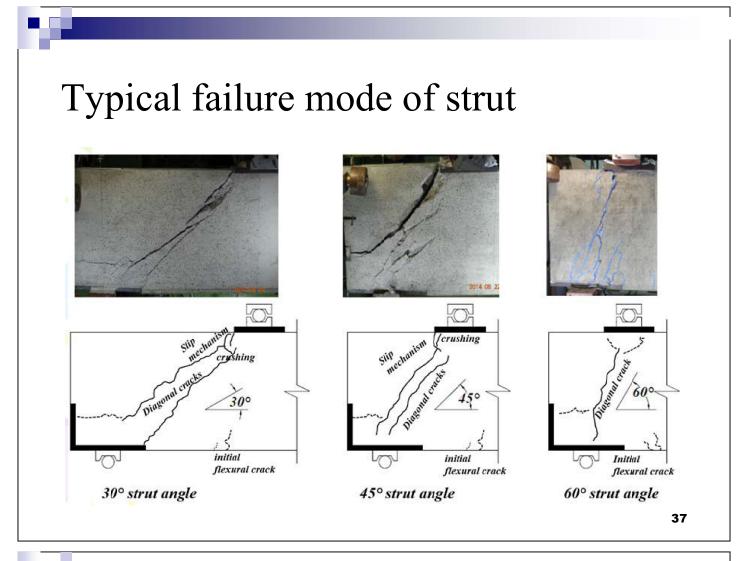
The localized effects caused by any load acting on the body will dissipate or smooth out within regions that are sufficiently away from the location of the stress concentration

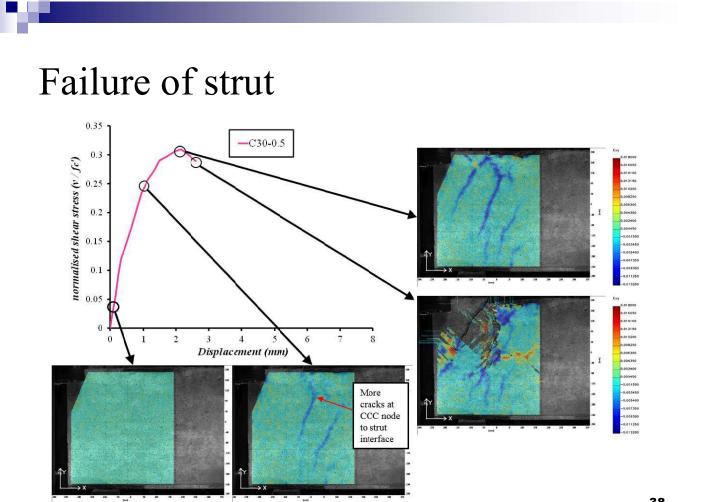


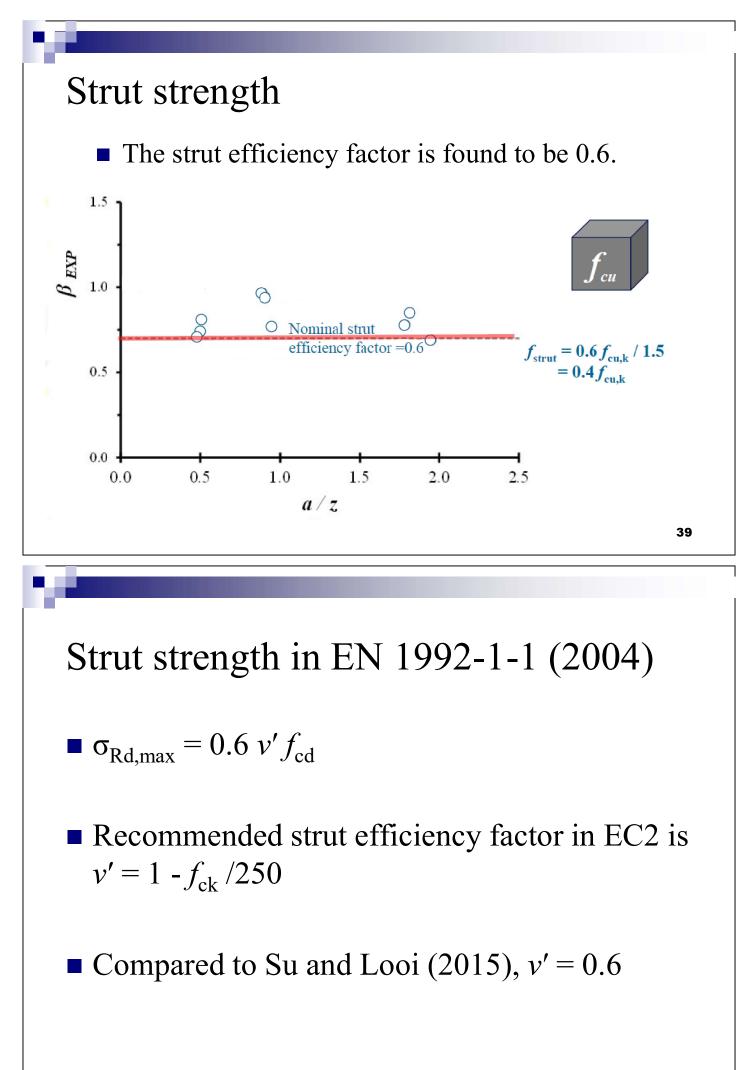
Zone of body affected by self equilibrium forces applied to surface

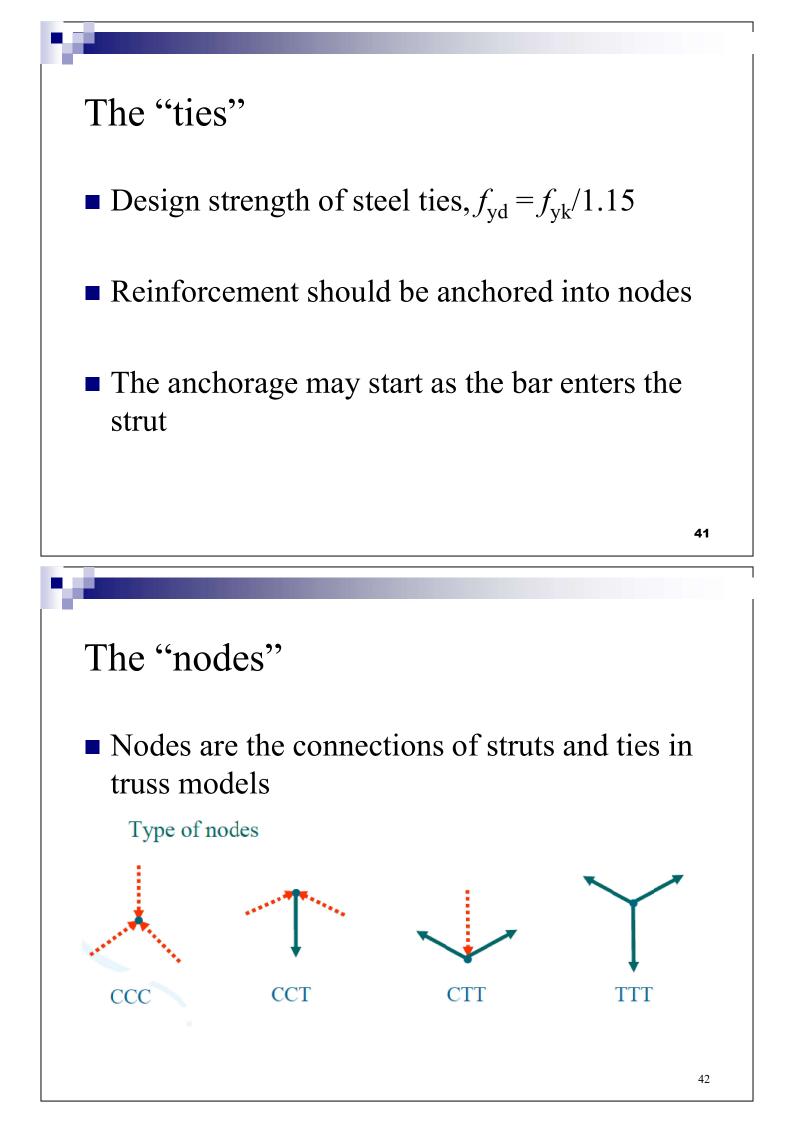


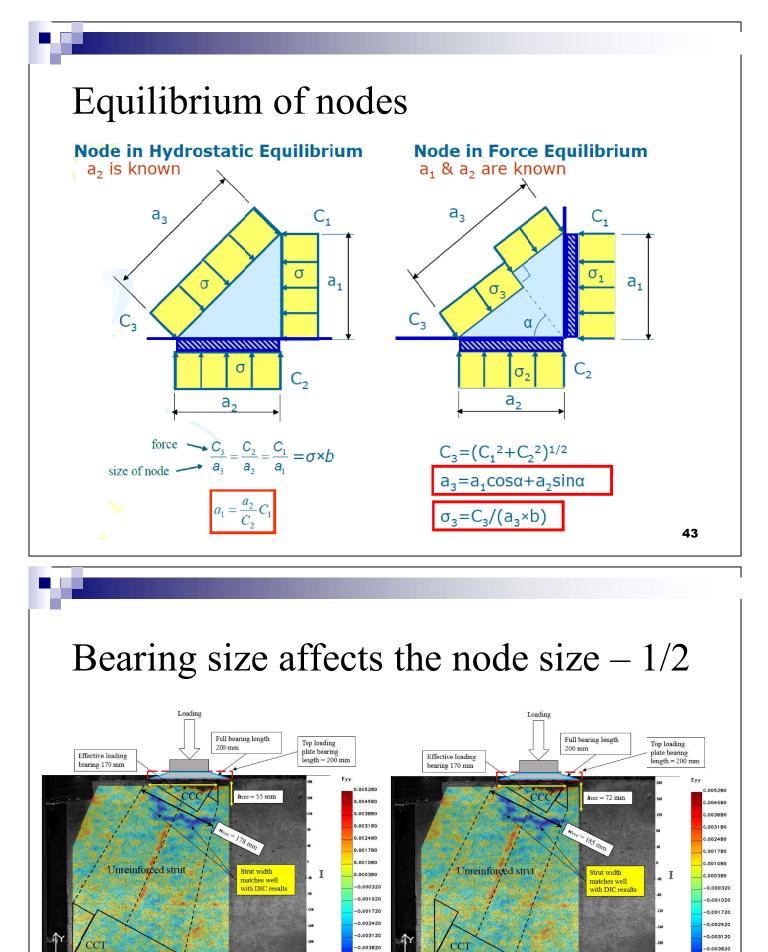














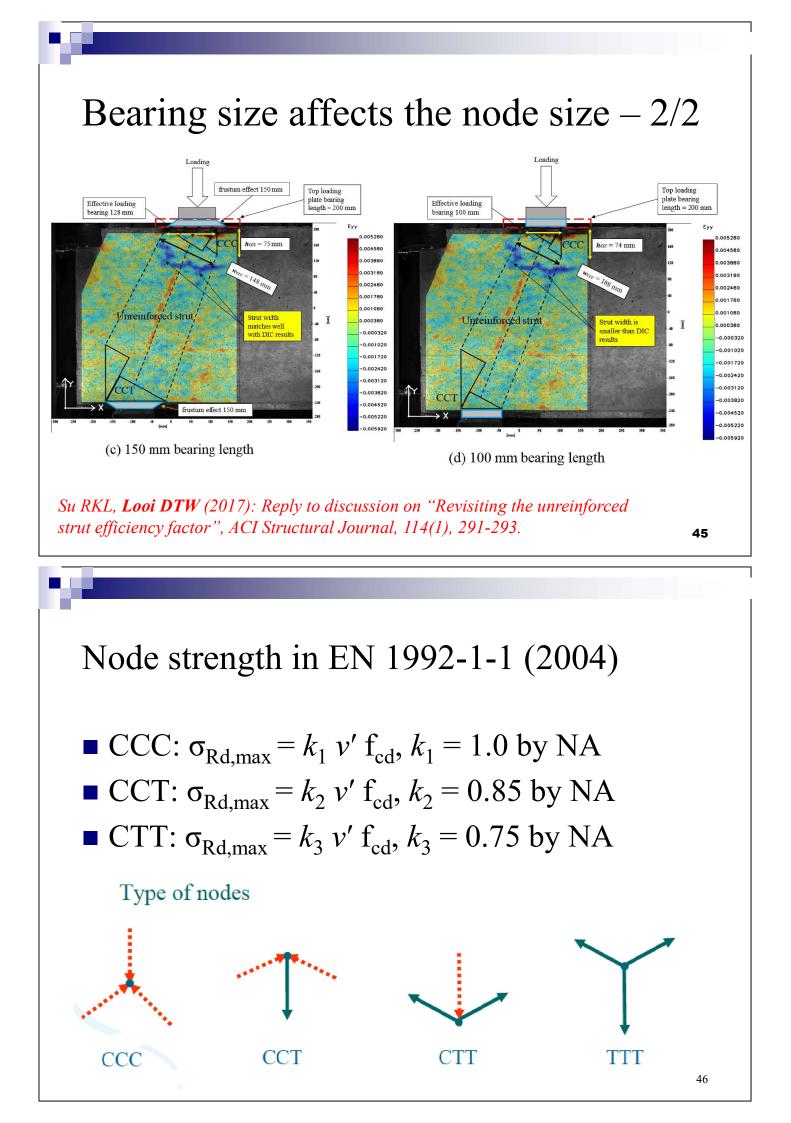
(b) 200 mm bearing length

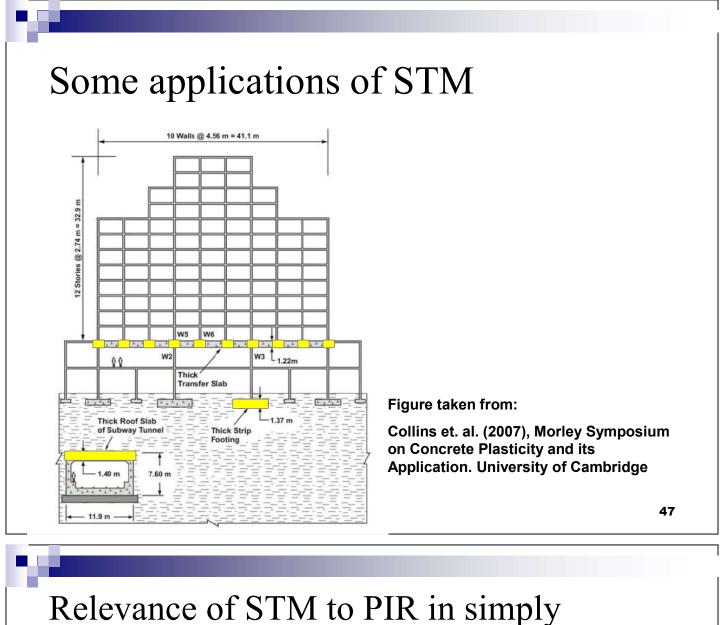
frustum effect 200 mm

-0.004520

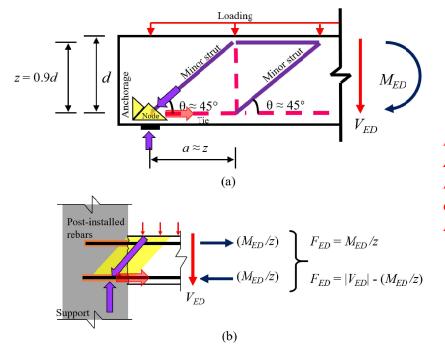
0.005220

0.005920

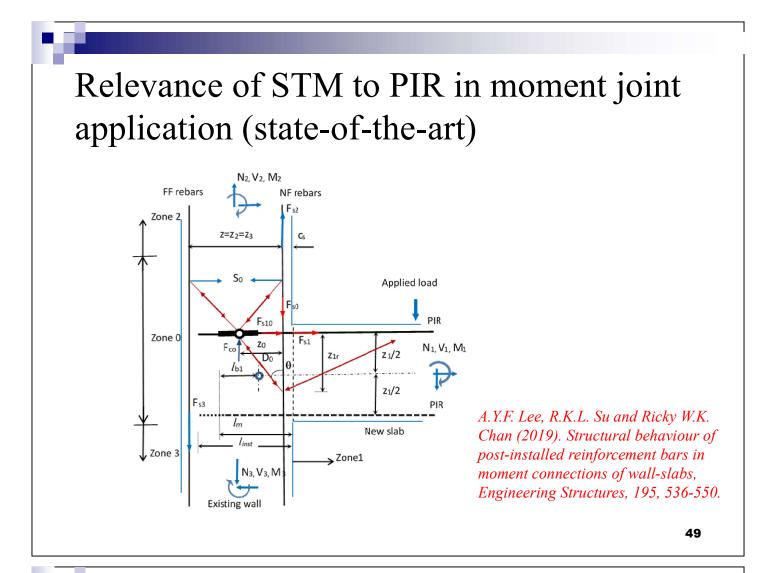




supported application



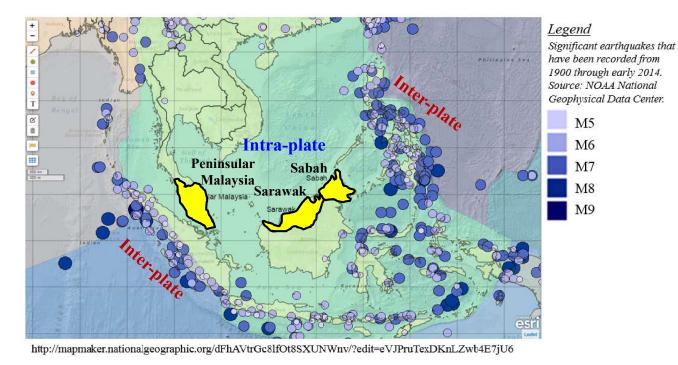
R.K.L. Su, **D.T.W Looi** and Y.L. Zhang (in press, 2019), Guide for Design, Installation and Assessment of Post-installed Reinforcement, HKU Press, Hong Kong.

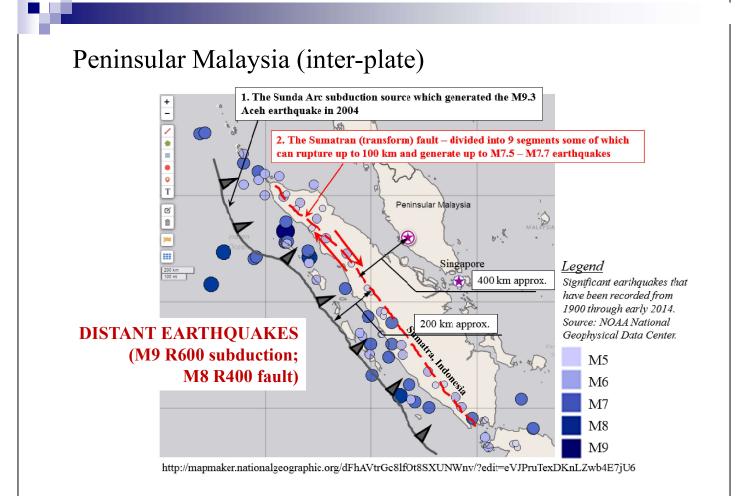


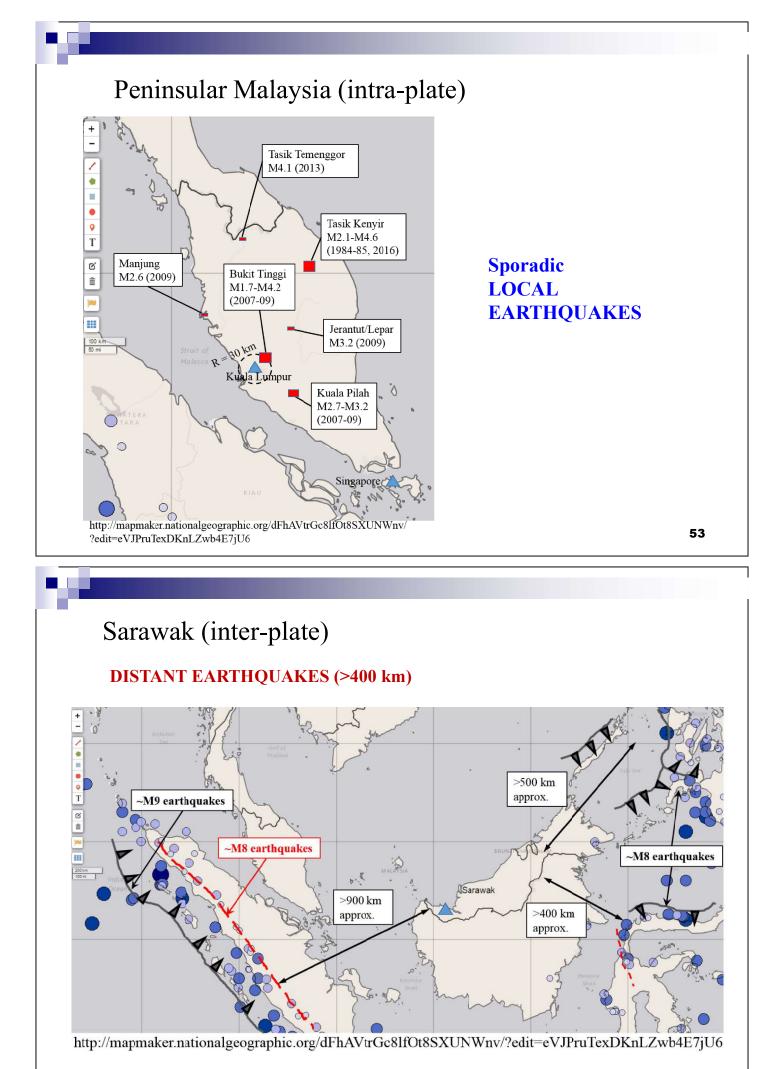
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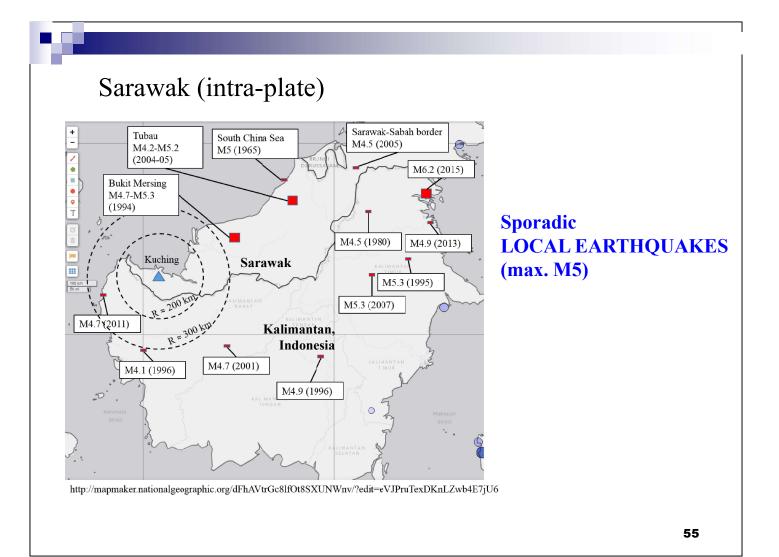
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- Design provision for Rebar End Anchorage Theory in EN 1992-1-1 (2004)
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## General seismic environment of Malaysia



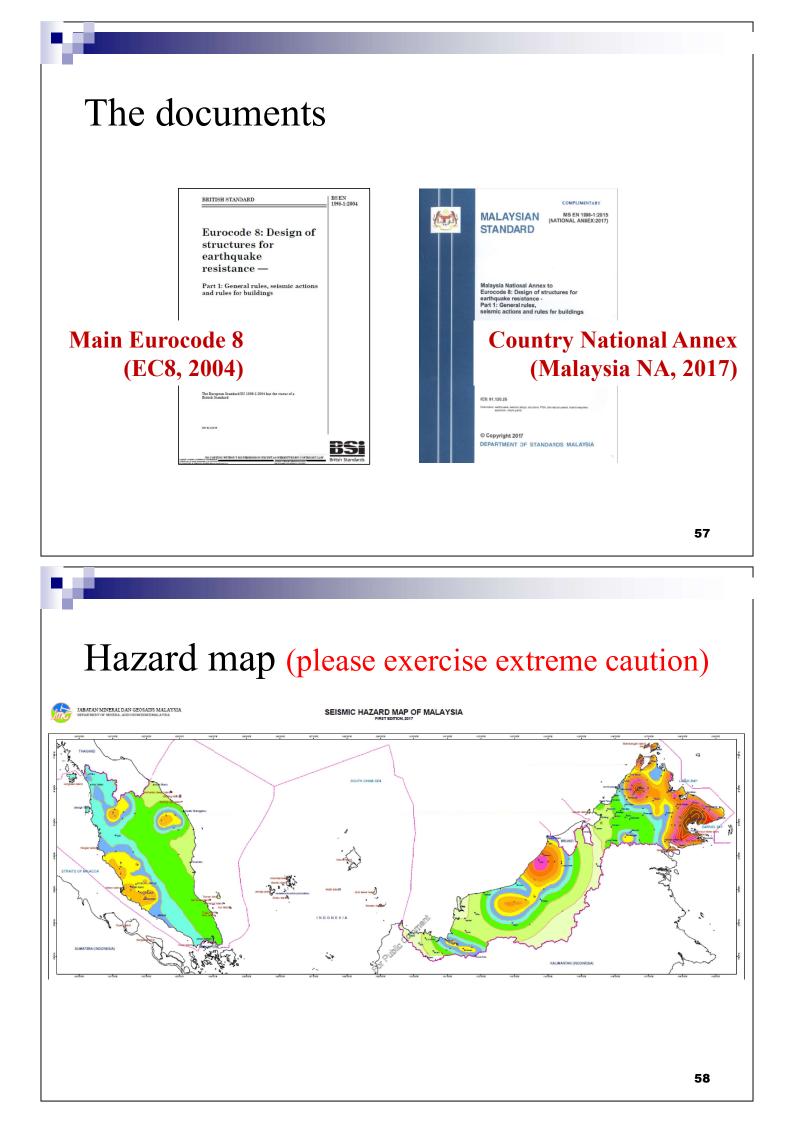






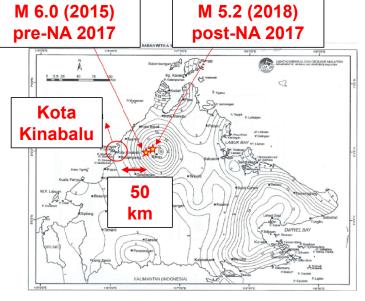
## Sabah (inter-plate & intra-plate)

M5.3, depth 33 km, M	ay 18, 1966 (USGS) -	
70 km to KK,	110'00'E	115'00'E 120'00'E
M5.4, depth 33 km, Ap	ril 28, 1973 (USGS) -	
185 km to KK, 👘 🗸		N X S
M5.3, depth 33 km, Ju	y 26, 1976 (USGS) -	
250 km to KK,	$\sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{j=1}^{n} \sum_{i=1}^{n} \sum_{i$	$X \times X $
M6.2, depth 33 km, Ju	y 26, 1976 (USGS) -	A Alian la
270 km to KK,	$\mathcal{M}^{(I)}$	A Standard A
M5.0, depth 33 km, Se	ptember 18, 1976	
(USGS) - 264 km to KK,		RETAILARD THE CONTRACT OF ALL STORE
M5.6, depth 50.3 km, I		Ranfrey to a
(USGS) - 270 km to KK,		A Traine frage to Name
M5.1, depth 79.4 km, I		Invances ( Interest )
(USGS) - 197 km to KK,		LEAMI I have a stranger of the
M5.1, depth 33 km, M	ay 26, 1991 (USGS) -	
70 km to KK, 🔗		
M5.7, depth 55.2 km, I		Anna James .
(USGS) - 300 km to KK,		man - I man
M5.1, depth 33 km, Ap	ril 07, 2002 (USGS) -	Active LOCAL
175 km to KK,	and the second of the	ACTIVE LOCAL
M5.3, depth 19 km, M	ay 23, 2005 (USGS) -	EARTHQUAKES
180 km to KK,	05 2015 (MMD)	DEADER
M5.9, depth 10 km, Ju	ne 05, 2015 (IVIMD) -	(max. M6)
60 km to KK,	10 2015 (USCS)	
M5.3, depth 11.85 km, -60 km to KK.	June 12, 2015 (05GS)	8 12.
-60 Km 10 KK.	1100015	115'00'E 12#00'E
picent	re Magnitude	
	1 - 3.9	dis.
	4 - 4.9	W CO E
	5-5.9	s
	6 - 6.9	0 62.5 125 250 375 500
		1:6,000,000
	7 - 7.9	



## Consequence of uncontrolled use of PSHA

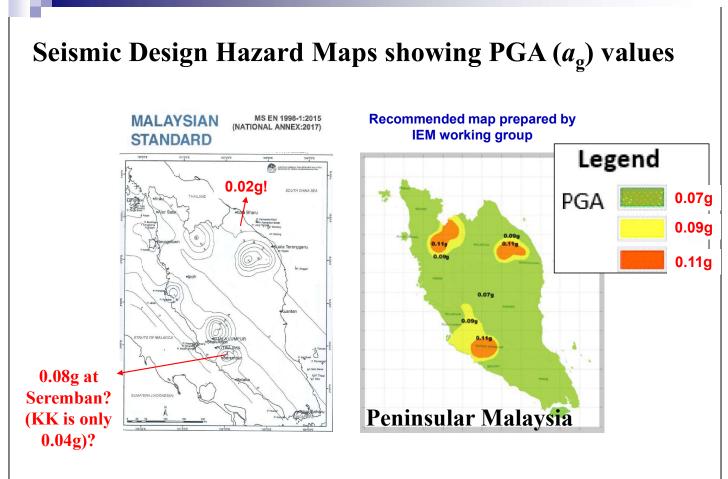
Records taken from https://earthquake.usgs.gov

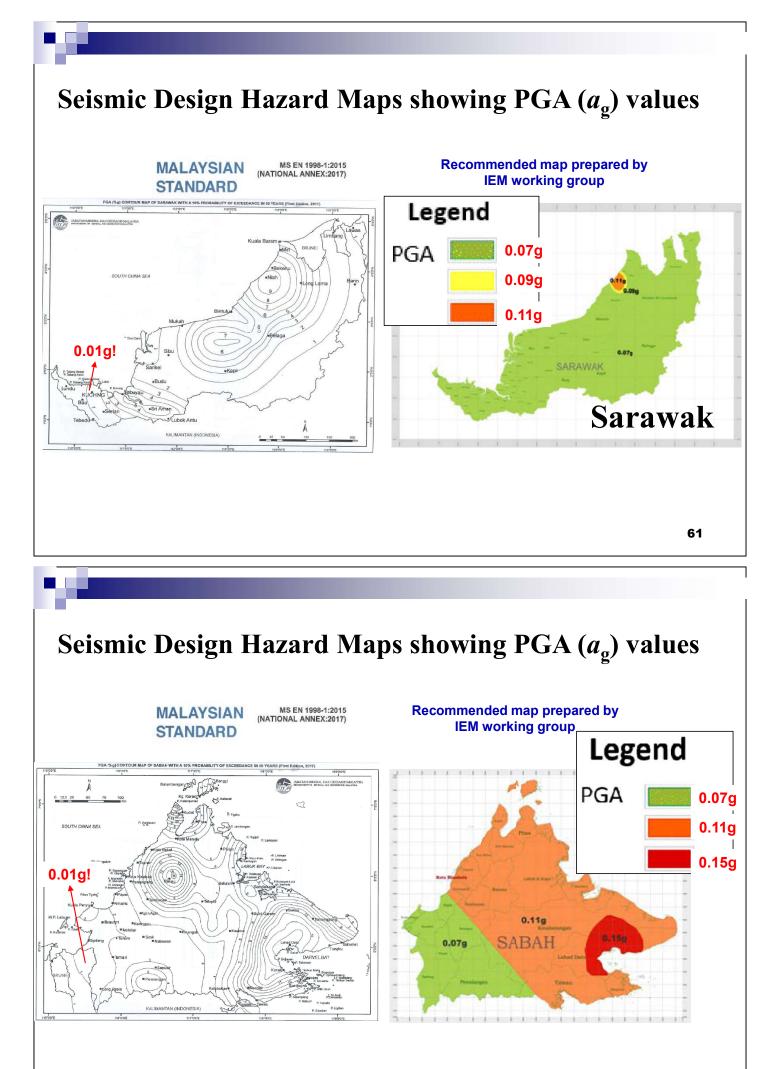


(a) Enacted version in National Annex (2017)

#### Consequence:

- Unacceptably low *PGA* value of 0.04g for *Kota Kinabalu* (capital city of *Sabah*)
- It is some 50 km from the epicentre of the M6.0 *Ranau* earthquake of 2015





## Qualification for seismic assessment of PIR

- The seismic action in Malaysia is quiet but not silent, we commonly termed as "low-to-moderate seismicity regions".
- Seismic assessment methods of can be found in EAD 331522 (endorsed draft 2018) in Europe and in AC 308 (2016) in the US.
- Engineers are reminded that it is essential to qualify the PIR system under static loading first as a prerequisite before proceeding to seismic assessment.

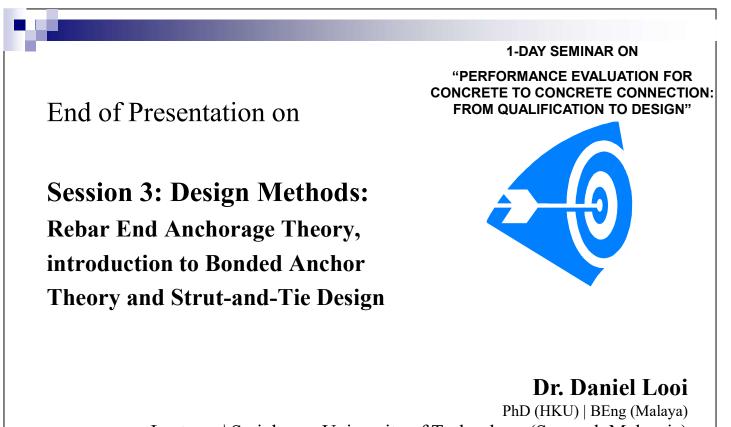
## Content

- 1. Design philosophy of PIR
- Design provision for Rebar End Anchorage Theory in EN 1992-1-1 (2004)
- Introduction to design provision for Bonded Anchor Theory in EN 1992-4 (2018)
- 4. Introduction to strut-and-tie model
- 5. Notes on seismic actions
- 6. Conclusion

## Conclusion

- The design philosophy of PIR was introduced
  - 1) REA Rebar End Anchorage as per EC2-1-1 (2004)
  - 2) BA Bonded Anchor as per EC2-4 (2018)
  - 3) STM Strut-and-Tie Model
- In REA, splitting failure was elaborated with an  $\alpha_2'$  method extended from EC2 for higher bond strength of adhesive.
- In BA, the complex formulation as per EC2-4 (2018) was introduced.
- In STM, definition of strut, tie and nodes were introduced with reference to the authors' ACI paper (2015) and EC2-1-1 (2004)
- Seismic actions in Malaysia was introduced together with PIR seismic assessment.

65



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